THE USE OF WPF FOR DEVELOPMENT OF INTERACTIVE GEOMETRY SOFTWARE

DAVORKA RADAKOVIĆ AND ĐORĐE HERCEG

Abstract. The Windows Presentation Foundation (WPF) is a graphical subsystem in .NET Framework 3.5, that uses a markup language, called XAML, for rich user interface development. Interactive geometry software (IGS) are computer programs that allow one to create and then manipulate geometric constructions, primarily in plane geometry. Some of the free well known 2D IGS are Geogebra, Cabri and Cinderella. Besides the intended use as a means of teaching and studying geometry, IGS are often used for other purposes, such as development of mathematical games or as a part of other mathematical software (e.g. mathematical drawing viewers). Thanks to its JavaScript interface, GeoGebra is often used in that role and controlled externally by some other software. However, there are some limitations to GeoGebra’s usefulness in that respect, since it wasn’t developed primarily for that purpose.

Our aim is to offer a solution that can be easily used as a software component for mathematical visualization and interaction. The framework we developed, called ”Geometrijica”, is simple, straightforward and extensible. It is based on the WPF, which enables it to have a rich graphical appearance and interactivity.

In this paper we demonstrate how our framework, when used together with a mathematical expression evaluator, can be used as a starting point for developing interactive mathematical software.

1. Introduction

Today there are many interactive geometry software (IGS) products available [1], [2], [3]. They are used mostly in teaching and studying geometry, and some more advanced IGS can also graph functions and their derivatives, perform algebraic and symbolic manipulations and so on.

The importance of IGS in today’s teaching is widely studied and recognized [9], [11]. For that reason, teachers team up with software developers in order to
create interactive teaching and learning materials. In order to reach wide audi-
ences, such as elementary school pupils and teachers, the resulting software must be affordable and able to run on various platforms.

GeoGebra is one such IGS, which has gained wide acceptance due to several fac-
tors: it is free, runs on all modern operating systems, it is constantly updated and improved, its user interface and user manual have been translated into more than 40 languages, there exist a number of examples and teaching materials freely available on the Internet, and GeoGebra applets can be embedded and used interactively in Web pages [10]. Most importantly, GeoGebra is easy and intuitive to use.

However, the situation is not so simple when it comes to developing new, stand-alone software that should use an existing IGS as a component. First of all, the licensing mode of the IGS in question may not permit such use, and even if it does, there may be some technical limitations or interoperability prob-
lems. On the other hand, there are commercial software packages which are more than suitable for such development [4], but the prices for development and run-
time versions of these packages may prohibit their widespread use. One of the possible approaches to this problem is to use tools, such as Adobe Flash [5] or OpenLaszlo [6], which are not primarily intended for geometrical applications, for development of mathematical teaching materials, games and examples.

In our previous work, we used GeoGebra to develop course materials [13], [14], primarily because it is a free software and therefore accessible to our target audience. However, we encountered some of GeoGebra’s limitations:

- Geometrical shapes in GeoGebra have properties, such as color, line width and shape of points, which can only be changed via the user interface. It would be much more useful if properties of geometrical shapes could get their values from the results of mathematical expressions. That way we could have visual indicators that change their appearance based on the state of the geometrical drawing. For example, an oval representing a set of even numbers could change its color or border width when all the appropriate elements (represented as points) are placed inside its bounds.
- GeoGebra can be controlled from an external program by means of its JavaScript interface. However, this interface, in its current state, provides only the basic functionality. We would like to be able to control every aspect of the geometrical drawing and to react to all the events, such as mouse clicks, keyboard pressed, or object overlapping.
- Properties of objects in GeoGebra are accessed by means of special func-
tions, unlike properties of objects in object-oriented programming lan-
guages, which we feel is a more natural way. For example, to obtain the x-coordinate of a point, one needs to type x(A) instead of A.x. This
method is awkward when there are a large number of properties, since each property requires a special function to access it.

- For mathematical game development, we often need to create customized graphical objects, such as coins, fruits, traffic lights, houses, cars etc. While this is possible in GeoGebra, it can be awkward and time consuming. Furthermore, it is not possible to create more than one instance of a customized graphical object needed in any other way but by drawing each instance separately.

For that reason, we decided to develop a new framework, which will solve these problems, while retaining all good aspects of GeoGebra. Since we already had developed a mathematical expression parser and evaluator in C#, we decided to base our framework on it. However, our solution can easily be adopted to use another computer algebra system. Windows Presentation Foundation (WPF) was chosen as the graphical subsystem.

2. Expression evaluator and parser

We developed an expression evaluator and parser, which are based on the same principles as the ones in GeoGebra.

**Expression** is any simple or complex expression which can be constructed by using constants, variables, arithmetic and logic operations, properties of objects and function calls. Supported functions include common mathematical functions such as power, trigonometry and logical functions. Basically, an Expression is what we are used to seeing in most programming languages like C#. Complex expressions are built by combining simpler expressions using function composition. Besides that, expressions are used to describe geometrical notions, their properties and relations. For example, if \( M = \text{Segment}(A, B) \) represents a segment between points A and B, then \( \text{Perpendicular}(M, M.\text{Midpoint}) \) represents a line perpendicular to \( M \), passing through its midpoint.

**Parser** is tasked with accepting textual input and transforming it into expressions. The syntax resembles expression syntax in C#, with arithmetic operations, function calls, and member access. Internally, arithmetic and logic operations and member access are transformed into function calls. For example, the input \( A = M.X + 3 \) is transformed into \( \text{SetVar}("A", \text{Plus}(\text{MemberOf}("M", "X"), 3)) \). Therefore, all evaluation is actually performed by executing functions.

Expressions have data types. Some common data types are: Number, String, Logical, Color, Point, Segment, Line, Circle and so on. Arguments of functions are checked for data type compatibility at execution. When an expression cannot be evaluated for any reason, it returns a value of the Error data type. Any expression depending on that value also returns a value of the Error data type. Variable is a named expression maintained by the evaluator. A variable consists of an expression and its result.
Variables can depend on other variables. For example, if \( M = \text{Segment}(A, B) \) is a segment between points A and B, and the coordinates of the point A change, then \( M \) must change accordingly. Evaluation of variables is dynamic. As soon as one variable changes its value, all dependent variables are reevaluated. Circular dependencies are not allowed. Therefore, the expressions \( A = f(B) \) and \( B = g(A) \) are not allowed at the same time. Table 2.1 shows the most important members of the Var class, which is used to keep variables in the evaluator. One important feature of the Var class is that it implements the INotifyPropertyChanged interface, which enables it to notify data consumers of changed values.

<table>
<thead>
<tr>
<th>public string Name</th>
<th>The name of the variable.</th>
</tr>
</thead>
<tbody>
<tr>
<td>public Expression Expr</td>
<td>The expression assigned to the variable.</td>
</tr>
<tr>
<td>public Expression Result</td>
<td>Result of evaluation of the variable.</td>
</tr>
<tr>
<td>public bool Valid</td>
<td>Indicates whether the result is valid.</td>
</tr>
<tr>
<td>public event PropertyChangedEventHandler PropertyChanged</td>
<td>Event from the INotifyPropertyChanged interface, which must be implemented in order to use this class as a data source.</td>
</tr>
</tbody>
</table>

Evaluator is a computational engine that keeps a set of named expressions and maintains dependencies between them, ensuring that when one expression changes, all dependent expressions get reevaluated. It also maintains the expression set in a consistent state by preventing creation of circular dependencies and by deleting all dependent expressions of a deleted expression.

3. Design goals

The requirements placed before the Geometrijica framework are the following:

- Mathematical notions that can be drawn on paper, such as points, lines, circles and graphs of functions, can be shown on screen. For example, by defining a variable \( M = \text{Segment}(A, B) \) we are also creating a graphical representation of the segment \( M \), which is drawn on screen. When the value of the variable changes, the image on the screen also changes.
- **Geometrical drawing** is a 2D image, consisting mostly of (but not limited to) geometrical shapes, such as points, lines and circles. It is kept in computer memory as a list of visual elements with their respective coordinates and other properties, such as color, size and border width.
- Any property of a visual element can be bound to any variable of the appropriate type. For example, the location of a point in the Cartesian coordinate system can depend on a variable of the type Point. When the value of the variable changes, the position of the visual element is updated on the screen.
• **Visual elements** can represent geometrical shapes, mathematical notions, but they can also be controls, such as buttons, check boxes or sliders. They are implemented by inheriting from WPF controls and user controls, or by inheriting from System.Windows.FrameworkElement. Existing functionality of inherited controls is retained.

• Dependency properties of WPF user controls can be bound to any variable of the appropriate type. Data types are converted by special converter classes. For each pair of types there exists a converter class that provides conversion between them. This enables creation of rich visual representations, which can be controlled by expressions from the evaluator. For example, one can develop a user control that displays a traffic light, with a property that specifies which light is on, and then animate the lights by binding the property to a variable in the evaluator.

• **GeoCanvas** is a WPF control that displays geometrical drawings. GeoCanvas inherits from System.Windows.Controls.Canvas. The part of the 2D plane that is shown inside the GeoCanvas is specified by the coordinates of the lower left and upper right corners. The area displayed in the GeoCanvas can be panned and zoomed.

• GeoCanvas supports both screen coordinate system and geometrical Cartesian coordinate system. Visual elements that are placed on a GeoCanvas decide which coordinate system they will use. Objects using screen coordinates do not move when the geometrical coordinate system moves. This facilitates mixing of user interface elements with the elements of a geometrical drawing.

4. IMPLEMENTATION

4.1. System overview. The structure of a program built on the Geometrijica framework is shown in Fig. 4.1. The scope of this discussion is limited to the Visuals, Conversion and Algebra packages, which correspond to appropriate namespaces in Geometrijica.

The Algebra package contains classes discussed in the section ”Expression evaluator and parser”. A partial list of the classes is shown in Table 4.1.

<table>
<thead>
<tr>
<th>Number, String, Logical, EColor</th>
<th>Data types</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neg, Plus, Times</td>
<td>Arithmetic operations</td>
</tr>
<tr>
<td>Sqrt, Power, Sin, Cos</td>
<td>Mathematical functions</td>
</tr>
<tr>
<td>EPoint, Segment, Line, Circle</td>
<td>Geometrical shapes</td>
</tr>
<tr>
<td>Evaluator</td>
<td>Calculation engine</td>
</tr>
<tr>
<td>Var</td>
<td>A variable, used in the calculation engine</td>
</tr>
</tbody>
</table>

Table 2. A partial list of classes in the Algebra namespace
The Visuals package contains the GeoCanvas class, which is a special Canvas control that supports the geometrical coordinate systems, besides the usual pixel-based screen coordinate system. The package also contains classes for graphical representation of geometrical notions, as well as other graphical classes and user interface elements, such as classes derived from WPF controls. The Conversion package contains converters which perform data type conversions necessary for data binding.

4.2. **Interfaces and enums.** Positioning mode of visual elements is determined by the LocationMode enumeration. The value Screen means that the location of an element is expressed in screen pixels, while the value Geometry means that the location is expressed in geometrical coordinates and that a conversion to screen coordinates is necessary before the element is drawn on screen.

```java
public enum LocationMode {
    Screen, Geometry
}
```

**Listing 1. LocationMode enumeration**

All visual elements must implement the IElement interface (Table 4.2), which provides basic functionality for element positioning and visibility control. The Valid property is used to control element’s visibility based on the validity of the expression it is bound to.

For example, let $M=$ Segment$(A, B)$ be a segment between the points $A$ and $B$, and $P=$ Perpendicular$(M, M.$Midpoint$)$ a line perpendicular to $M$, passing through its midpoint. Suppose that both $M$ and $P$ have their corresponding visual elements shown on screen. Then, if the points $A$ and $B$ are equal, the length of the segment $M$ is zero and the line $P$ cannot exist. In that case, the value of
the variable P in the evaluator will be marked as invalid, and the visual element corresponding to P should not be drawn. This is accomplished by binding the Valid property of the visual element to the Valid property of the variable in the evaluator.

<table>
<thead>
<tr>
<th>GeoCanvas GeoCanvas</th>
<th>The GeoCanvas object this element belongs to. Elements use this reference to obtain information about geometrical coordinates in the GeoCanvas.</th>
</tr>
</thead>
<tbody>
<tr>
<td>bool Valid</td>
<td>Determines whether the element is valid, i.e. whether it should be drawn.</td>
</tr>
<tr>
<td>public Expression Result</td>
<td>Result of evaluation of the variable.</td>
</tr>
<tr>
<td>bool Visible</td>
<td>Controls visibility of the element.</td>
</tr>
<tr>
<td>void CalcScrLocation()</td>
<td>Calculates and updates the location of the visual element on the screen.</td>
</tr>
</tbody>
</table>

Table 3. Members of the IElemnet interface

```
private GeoCanvas _geoCanvas;
public GeoCanvas GeoCanvas
{
    get { return _geoCanvas; }  
    set { _geoCanvas = value;  }
}
public void CalcScrLocation()
{
    if (GeoCanvas != null)
    {
        switch (LocationMode)
        {
            case LocationMode.Geometry:
                ScrLocation = GeoCanvas.Geo2Scr(Location);
                break;
            case LocationMode.Screen:
                ScrLocation = Location;
                break;
        }
    }
}
```

Listing 2. A typical IElemnet implementation in a visual element class

The ILocation interface (Table 4.3) should be implemented by visual elements which can choose the positioning mode between LocationMode.Screen and LocationMode.Geometry. Most visual elements that represent geometrical shapes do not implement this interface. On the other hand, user interface elements such as buttons, check boxes and sliders, which can be placed either on fixed location on screen or bound to geometrical coordinates, implement the ILocation interface.
4.3. GeoCanvas. The GeoCanvas class extends the System.Windows.Controls.Canvas class. It represents a view of a 2D plane in the Cartesian coordinate system. GeoCanvas has four properties, named X0, Y0, X1 and Y1, which determine the region of the 2D plane that is shown on the GeoCanvas.

Visual elements are added to the GeoCanvas by calling the RegisterVisual method.

The Geo2Scr method is used to convert geometrical coordinates into screen coordinates. This method is called by child visual elements, when they are requested by the GeoCanvas to determine their locations. Obviously, only the elements in the ‘geometry’ positioning mode use this method.

<table>
<thead>
<tr>
<th>Table 4. Members of the ILocation interface</th>
</tr>
</thead>
<tbody>
<tr>
<td>Point Location</td>
</tr>
<tr>
<td>LocationMode LocationMode</td>
</tr>
</tbody>
</table>

4.4. Dependency properties and data binding. The main idea in our work is to create visual elements which react dynamically to changes in expression values in the evaluator. WPF data binding [7] provides a simple and consistent way of binding elements to data sources, such as databases, XML documents, CLR objects etc.

In our case, data sources are evaluator variables (objects of type Var, Table 2.1). These objects implement the INotifyPropertyChanged interface, which takes care of notifying the WPF infrastructure when a property of a variable changes.
changes. Typical scenario is as follows. When a visual element is created, its properties are bound to the appropriate properties of the corresponding Var object. The visual element is then placed on a GeoCanvas and thus displayed on screen. Each subsequent change of Var object’s properties causes the data binding infrastructure to change corresponding properties of the visual element, which is displayed immediately on screen. For this purpose, one-way data binding is used.

Since the data types used in the Evaluator are different from those used in the visual elements, converters must be implemented for each pair of data types for which data binding is meaningful. Listing 3 shows the EPointConverter class, which converts values of type EPoint into values of type Point.

```csharp
[ValueConversion(typeof(EPoint), typeof(Point))]
public class EPointConverter : IValueConverter
{
    public object Convert(object value, Type targetType, object parameter,
                           System.Globalization.CultureInfo culture)
    {
        EPoint ep = value as EPoint;
        if ((ep != null) && (targetType.Equals(typeof(Point))))
        {
            double x1 = ((Number)ep.X).Value;
            double y1 = ((Number)ep.Y).Value;
            return new Point(x1, y1);
        }
        else
        {
            throw new ArgumentException("Invalid type. EPoint expected.", "value");
        }
    }

    public object ConvertBack(object value, Type targetType, object parameter, System.Globalization.CultureInfo culture)
    {
        (code omitted)
    }
}
```

Listing 3. A partial listing of the DoubleConverter class

Listing 4 shows lines of code that bind the result of the evaluator variable A to the first point of the segment sg. After this code has executed, all changes in the result of the variable A will be immediately reflected on the drawing on screen.

```csharp
sg = new VSegment(new Point(0, 0), new Point(3, 5));
GeoPanel1.RegisterVisual(sg);
Binding bA = new Binding("Result");
bA.Source = Evaluator.Default.Variables["A"];  // "A" is a variable name
sg.SetBinding(VSegment.AProperty, bA);
```

Listing 4. Binding of an evaluator variable to a visual element
4.5. **Visual Elements.** Visual elements are objects that are actually drawn on GeoCanvas. They can be simple dots and lines, or complex drawings. Besides that, common WPF controls, such as buttons, check boxes and sliders can be turned into visual elements and placed on GeoCanvas, while retaining all their functionality. Even complex user controls, with graphical effects and animations can be turned into visual elements and used.

![Visual Elements Diagram](image)

**Figure 3.** Visual elements VPoint, VSegment and VButton.

The process of making a new visual element is different depending on what class is chosen as a starting point. We can start from System.Windows.FrameworkElement and program everything by hand, or we can start from either Control, UserControl or one of the existing WPF controls and implement only a few necessary methods. In either case, the IElement interface must be implemented.

4.5.1. *Creating a new visual element from FrameworkElement.* In this section, the steps necessary to create a visual element from FrameworkElement will be explained. The VPoint class represents a geometrical point and it is drawn as a small circle on screen. The important members of the VPoint class are explained in Table 4.4.
Table 5. Important members of the VPoint class

<table>
<thead>
<tr>
<th>Method/Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>public GeoCanvas GeoCanvas</td>
<td>The GeoCanvas object this VPoint belongs to.</td>
</tr>
<tr>
<td>private static void RegisterProperties()</td>
<td>Registers dependency properties and their corresponding event handlers. Called from the static constructor.</td>
</tr>
<tr>
<td>public Point Location</td>
<td>Location of the geometrical point, either in screen or geometry coordinates.</td>
</tr>
<tr>
<td>public LocationMode LocationMode</td>
<td>Specifies how the location property is interpreted.</td>
</tr>
<tr>
<td>public double Size</td>
<td>Size of this VPoint in pixels.</td>
</tr>
<tr>
<td>protected override void OnRender(DrawingContext drawingContext)</td>
<td>Called by the WPF when the VPoint needs to be drawn.</td>
</tr>
<tr>
<td>private DrawingVisual DrawIt()</td>
<td>Performs actual drawing of the VPoint in the specified DrawingContext.</td>
</tr>
<tr>
<td>public int VisualChildrenCount</td>
<td>Required by the FrameworkElement specification. These methods must be implemented in all classes deriving from the System.Windows.FrameworkElement class.</td>
</tr>
<tr>
<td>public void AddVisual(Visual v)</td>
<td></td>
</tr>
<tr>
<td>public int VisualChildrenCount</td>
<td></td>
</tr>
</tbody>
</table>

To implement a geometrical point, we start by inheriting the FrameworkElement class. The methods VisualChildrenCount, AddVisual, DeleteVisual and GetVisualChild must be implemented as specified in [8].

We also implement the IElement interface, and the optional ILocation interface. Actual drawing of the point takes place in the DrawIt method, which is called when needed from the overridden OnRender method. The VPoint class has properties that determine its visual appearance. We will consider only the Size property, as implementation details are similar for all other such properties.

```csharp
static VPoint()
{
    RegisterProperties();
}

private static void RegisterProperties()
{
    FrameworkPropertyMetadata mdSize =
        new FrameworkPropertyMetadata(8.0, FrameworkPropertyMetadataOptions.AffectsRender,
                                        new PropertyChangedCallback(OnSizeChanged));

    SizeProperty =
        DependencyProperty.Register("Size", typeof(double), typeof(VPoint), mdSize);

    (code omitted)
}

public static DependencyProperty SizeProperty;

public double Size
{

get { return (double)GetValue(SizeProperty); }
set { SetValue(SizeProperty, value); }
}

private static void OnSizeChanged(DependencyObject obj,
    DependencyPropertyChangedEventArgs e)
{
    VPoint t = (VPoint)obj;
    t.DrawIt();
}

private DrawingVisual DrawIt()
{
    DrawingVisual vis = (DrawingVisual)visuals[0];
    using (DrawingContext dc = vis.RenderOpen())
    {
        // selection circle
        Brush sbr = new SolidColorBrush(Colors.Orange);
        sbr.Opacity = SelectionOpacity;
        Pen sp = new Pen(sbr, 5.5);
        dc.DrawEllipse(null, sp, ScrLocation, Size + 4, Size + 4);

        // shape of the point
        Brush br = Brushes.Blue;
        Pen p = new Pen(br, 2.0);
        dc.DrawEllipse(br, p, ScrLocation, Size, Size);
    }
    return vis;
}

Listing 5. Implementation of the Size property and the DrawIt method

Figure 4.4 shows the sequence diagram for the RegisterVisual method. When a new visual element (VPoint in this case) is added to the GeoCanvas via the RegisterVisual method, the GeoCanvas control invokes the CalcScrLocation method from the IElement interface. Since the VPoint in question is in the geometry positioning mode, it calls the Geo2Scr method of the GeoCanvas, in order to transform its geometrical coordinates into screen coordinates. After that, the OnRender method is invoked, which, in turn calls the DrawIt method. This method performs the actual drawing of the point at the screen coordinates.

4.5.2. Creating visual elements from existing controls. WPF controls already have full functionality, in other words, they know how to draw themselves and to react to user interaction, such as keyboard actions and mouse clicks. It is much easier to create visual elements from existing WPF controls than to code all drawing and behavior logic by hand, as is the case with visual elements based on FrameworkElement. In order to make a visual element from the Button class, we only need to implement the IElement interface in the inheriting class. If we want to be able to place the button on geometrical coordinates, as well as on screen coordinates, we should implement the ILocation interface too. Figure 4.3 shows the VButton class, which was created in the described way.
4.5.3. Creating visual elements from UserControl. As WPF controls can be specified in XAML, it is also possible to create visual element in that way. Listing 6 shows the specification of a traffic light control with three controllable lights, which can be switched on and off by setting the TrafficLight.Light dependency property. Since the TrafficLight control also implements the IElement interface, it can be placed on GeoCanvas in the same way as all other visual elements, and its appearance can be controlled by a variable from the evaluator (Figure 4.5).

```xml
<UserControl x:Class="HMS.Geometrijica.Visuals.TrafficLight"
    xmlns="http://schemas.microsoft.com/winfx/2006/xaml/presentation"
    xmlns:x="http://schemas.microsoft.com/winfx/2006/xaml"
    Height="90" Width="30">
    <Border BorderBrush="#FFDA1818" BorderThickness="3,3,3,3">
        <Grid x:Name="LayoutRoot" Background="#FFDDCECE">
            <Grid.RowDefinitions>
                <RowDefinition/>
                <RowDefinition Height="*"/>
                <RowDefinition/>
            </Grid.RowDefinitions>
            <Grid.ColumnDefinitions>
                <ColumnDefinition/>
            </Grid.ColumnDefinitions>
            <Ellipse Fill="#000000" Stroke="#FF000000" Grid.Row="0" x:Name="RedLight" Opacity="100"/>
            <Ellipse Fill="#000000" Stroke="#FF000000" Grid.Row="1" x:Name="YellowLight" Opacity="100"/>
            <Ellipse Fill="#FFFF3304" Stroke="#FF000000" Margin="3 3 3 3" Grid.Row="0" x:Name="GreenLight" Opacity="100"/>
        </Grid>
    </Border>
</UserControl>
```
Listing 6. Specification of the TrafficLight control in XAML

One benefit from creating visual elements from existing controls is that these elements retain full functionality of the controls they are based on. This way, we can mix geometrical shapes with WPF controls on a GeoCanvas control. Furthermore, dependency properties of those controls can be bound to results of arbitrary expressions in the evaluator (provided that appropriate converters exist).

4.6. Example. Figure 4.5 shows a simple window, containing a GeoCanvas control, which in turn contains three TrafficLight controls at screen coordinates, and one point, one segment and one button at geometrical coordinates. When the GeoCanvas is resized, panned and zoomed, the traffic light controls retain their positions, while the other controls’ positions move accordingly.

![Figure 5. Point, segment, button and three traffic light controls on a GeoCanvas.](image)

5. Conclusion

Existing interactive geometry software (IGS) are used in teaching of geometry and mathematics in general. GeoGebra is one IGS that has gained wide acceptance thanks to its intuitive use and a great range of features. However, GeoGebra cannot without difficulty be used as a component in other software products. Therefore we developed the ‘Geometrijica’ framework for geometry software development. A significant part of our framework is the graphical subsystem, which can display geometrical shapes, WPF controls and user controls at the same time.
By using dependency properties and data binding infrastructure in the WPF, we have managed to link the calculation engine with the graphical subsystem, so that all changes in calculation results are reflected in the geometrical drawing. We have also demonstrated that any property of a visual object can be bound to an arbitrary expression in the calculation engine, which is a step further from what GeoGebra offers in this respect. Also we have demonstrated how new visual objects can be made, either by programming them from scratch or by inheriting existing controls. By following a few simple rules, new visual objects can easily be created and used in geometrical drawings. Geometrijica can easily be used as a component in other programs.

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DEPARTMENT OF MATHEMATICS AND INFORMATICS, FACULTY OF SCIENCES, TRG DOSITEJA OBRADOVIĆA 4, 21000 NOVI SAD, SERBIA
E-mail address: davorkar@dmi.uns.ac.rs

DEPARTMENT OF MATHEMATICS AND INFORMATICS, FACULTY OF SCIENCES, TRG DOSITEJA OBRADOVIĆA 4, 21000 NOVI SAD, SERBIA
E-mail address: herceg@dmi.uns.ac.rs

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